

Primera serie

(Castellan 12^a Edición)

18.7)

Datos:

$$r = ? \quad \rho_{\text{agua}} = 1 \text{ g/cm}^3 \quad \theta = 0 \quad \gamma = 73 \times 10^{-3} \text{ N/m}$$

Se desprecia la presión del aire

$$r = \frac{2(\cos \theta) \gamma}{\rho h g} \rightarrow \frac{2(\cos 0^\circ) 73 \times 10^{-3}}{1(30)(9.8)} = 4.9609 \times 10^{-4} \text{ m}$$

18.9)

Datos:

$$r = 0.05 \text{ cm} \quad \gamma = 0.072 \text{ N/m} \quad \Delta P = P$$

$$L = 0.0005 \text{ m}$$

Despreciar la profundidad de inmersión

$$\Delta P = \frac{2\gamma}{r} \rightarrow \frac{2(0.072)}{0.0005} = 288 \text{ Pa}$$

18.13)

Datos:

$$T = 20^\circ \text{C} \quad \gamma_{\text{benzene}} = 28.85 \text{ mN/m} \quad \gamma_{\text{agua}} = 72.75 \text{ mN/m}$$

$$\theta = 0^\circ \quad \gamma_{\text{int}} = 35 \text{ mN/m}$$

Determinar

- Trabajo de adhesión entre el agua y el benceno
- Trabajo de cohesión para el benceno y para el agua
- Coefficiente de cohesión para el benceno y el agua

$$a) W_{ad} = \gamma_{agua} + \gamma_{benceno} + \gamma_{int} \rightarrow 72.75 \times 10^{-3} + 28.25 \times 10^{-3} + 35 \times 10^{-3} = 0.1366 \text{ N/m}$$

$$b) W_{coh} = 2\gamma$$

$$A_{agua} = 2(72.75 \times 10^{-3}) = 0.1455 \text{ N/m} \quad Benceno = 2(28.25 \times 10^{-3}) = 0.05775 \text{ N/m}$$

c)

18.19)

Acido esteárico ($C_{17}H_{35}(COO)_2$) $\rho = 0.85 \text{ g/cm}^3$ $A = 0.205 \text{ nm}^2$
 $\hookrightarrow 284 \text{ g/mol}$
 $L = ?$

$$\bar{v} = \frac{M}{\rho} = \frac{284 \text{ g/mol}}{0.85 \text{ g/cm}^3} = 334.11 \text{ cm}^3/\text{mol} \left(\frac{1 \text{ m}^3}{10^6 \text{ cm}^3} \right) = 3.3411 \times 10^{-4} \text{ m}^3$$

$$\bar{v}_{molecule} = \frac{\bar{v}}{N_A} = \frac{3.3411 \times 10^{-4} \text{ m}^3/\text{mol}}{6.022 \times 10^{23} \text{ molecules/mol}} = 5.548 \times 10^{-28} \text{ m}^3$$

$$\hookrightarrow \left(\frac{10^{27} \text{ nm}^3}{1 \text{ m}^3} \right) = 0.5548 \text{ nm}^3$$

$$\bar{v}_{molecule} = A \cdot L$$

$$L = \frac{\bar{v}_{molecule}}{A_{molecule}} = \frac{0.5548 \text{ nm}^3}{0.205 \text{ nm}^2} = 2.7 \text{ nm}$$

18.25)

a) Acido acetico en agua a 30°C $PM = 60 \text{ g/mol}$

% peso de acido	2.475	5.001	10.01	30.09	49.96	69.91
$\gamma (10^{-3} \text{ N/m})$	64.4	60.1	54.6	43.6	38.4	34.3

Graticar γ en funcion de $\ln m$ y determinar el exceso superficial del acido acetico usando la isoterma de adsorcion de Gibbs

b) Acido propionico en agua a 25°C $PM = 74 \text{ g/mol}$

% peso de acido	1.91	5.34	9.8	21.7
$\gamma (10^{-3} \text{ N/m})$	60	49	44	36

$$a) \frac{2.475 \text{ g}}{60 \text{ g/mol}} = 4.125 \times 10^{-3} \text{ mol} \quad \frac{5.001 \text{ g}}{60 \text{ g/mol}} = 0.08335 \text{ mol}$$

$$\frac{10.01 \text{ g}}{60 \text{ g/mol}} = 0.167 \text{ mol} \quad \frac{30.09 \text{ g}}{60 \text{ g/mol}} = 0.5015 \text{ mol}$$

$$\frac{49.96 \text{ g}}{60 \text{ g/mol}} = 0.832 \text{ mol} \quad \frac{69.91 \text{ g}}{60 \text{ g/mol}} = 1.165 \text{ mol}$$

$$4.125 \times 10^{-3} - \frac{97.525 \text{ g}}{1000 \text{ g}} = 0.0423 \quad 0.08335 - \frac{94.999 \text{ g}}{1000 \text{ g}} = 0.877$$

$$0.167 - \frac{89.99 \text{ g}}{1000 \text{ g}} = 1.855 \quad 0.5015 - \frac{69.91 \text{ g}}{1000 \text{ g}} = 7.173$$

$$0.832 - \frac{50.04 \text{ g}}{1000 \text{ g}} = 16.626 \quad 1.165 - \frac{30.09 \text{ g}}{1000 \text{ g}} = 38.777$$

$m(C_2)$	$\ln x$	$\gamma (10^{-3} N/m)$
0.0422	-3.165	64.4
0.277	-0.131	60.1
1.355	0.61	54.6
7.173	1.97	43.6
16.626	2.81	38.4
36.717	3.626	34.3

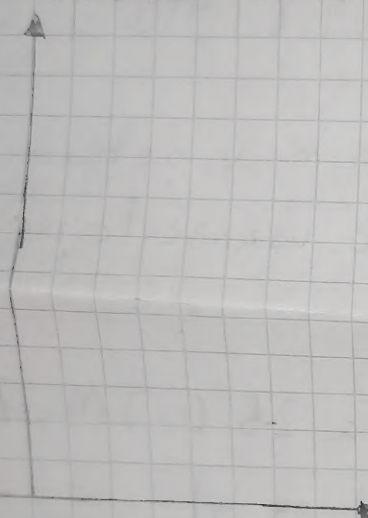
$$A = 53.759$$

$$B = -4.747 \times 10^{-3} N/m$$

$$r = -0.942$$

$$\Gamma_2 = \frac{-(-4.747 \times 10^{-3})}{(2.314)(303.15)}$$

$$= 1.223 \mu mol/m^2$$



b)

$$\frac{1.91g}{74g/mol} = 0.0258 mol \quad \frac{5.84g}{74g/mol} = 0.0789 mol$$

$$\frac{9.2g}{74g/mol} = 0.1324 mol \quad \frac{21.7g}{74g/mol} = 0.2932 mol$$

$$0.0258 - \frac{9.2 \times 10^{-4} s}{1000s} = 0.263 \quad 0.0789 - \frac{94.16 \times 10^{-4} s}{1000s} = 0.8379$$

$$0.1324 - \frac{90.2 \times 10^{-4} s}{1000s} = 1.4678 \quad 0.2932 - \frac{78.3 \times 10^{-4} s}{1000s} = 3.7445$$

$m(C_2)$	$\ln x$	$\gamma (10^{-3} N/m)$
0.263	-1.3356	60
0.8379	-0.1756	49
1.4678	0.3837	44
3.7445	1.3202	36

$$A = 47.6858$$

$$B = -9.0475$$

$$r = -0.9996$$

$$\Gamma_2 = \frac{-(-9.0475 \times 10^{-3})}{(2.3145)(298.15)}$$

$$= 3.6497 \mu mol/m^2$$

Atkins (3^{ra} edición)

A7.9)

$$T = 20^{\circ}\text{C} \quad M = 154 \text{ g/mol}$$

$$\gamma_{\text{oclu}} = 0.027 \text{ N m}^{-1}$$

$$\rho = 1.6 \text{ g/cm}^3$$

$$P^* = 87.05 \text{ Torr} \quad P = 87.95 \text{ Torr}$$

$$\gamma = \frac{2\gamma\bar{V}}{RT \ln(P/P^*)} \quad \bar{V} = \frac{M}{\rho} = \frac{154 \text{ g/mol}}{1.6 \text{ g/cm}^3} = 96.25 \text{ cm}^3 \times \frac{1 \text{ m}^3}{10^6 \text{ cm}^3} = 9.625 \times 10^{-5} \text{ m}^3$$

$$r = \frac{2(0.027 \text{ N m}^{-1})(9.625 \times 10^{-5} \text{ m}^3)}{(8.314 \frac{\text{J}}{\text{mol K}})(293.15 \text{ K}) \ln(\frac{87.95 \text{ Torr}}{87.05 \text{ Torr}})} = 2.07 \times 10^{-7} \text{ m}$$

A7.10)

$$P_{\text{int}} = ? \quad P_{\text{ext}} = 740 \text{ Torr} \quad r = 0.125 \text{ mm} \quad \gamma = 5.7 \times 10^{-2} \text{ N/m}$$

$L > 0.00125 \text{ m}$

Calcular presión interna de la burbuja

$$\Delta P = \frac{2\gamma}{r} \rightarrow P_{\text{int}} - P_{\text{ext}} = \frac{2\gamma}{r} \rightarrow P_{\text{int}} = \frac{2\gamma}{r} + P_{\text{ext}}$$

$$P_{\text{int}} = \left(\frac{2(5.7 \times 10^{-2} \text{ N/m})}{1.25 \times 10^{-4} \text{ m}} \right) + 740 \text{ Torr} = 1652 \text{ Torr}$$

7.39) En cuanto cambia la presión de vapor del benceno cuando este se dispersa en forma de pequeñas gotas de radio a) $10\mu\text{m}$, b) $0.10\mu\text{m}$ a 25°C ?

7.41)

$$A_{\text{succ}} \quad h = \frac{2\gamma}{\rho r g}$$

$$\gamma = 7.22 \times 10^{-2} \text{ N/m (a } 20^\circ\text{C)} \quad \gamma = 5.8 \times 10^{-2} \text{ N/m (a } 100^\circ\text{C)}$$

$$\rho = 0.998 \text{ g/cm}^3 \rightarrow 998 \text{ kg/m}^3 \quad \rho = 0.958 \text{ g/cm}^3 \rightarrow 958 \text{ kg/m}^3$$

Calcular elevación en tubos de a) 1mm b) 0.1mm de radio
 $\hookrightarrow 0.001\text{m} \quad \hookrightarrow 0.0001\text{m}$

$$\frac{2(5.8 \times 10^{-2} \frac{\text{kg} \cdot \text{m}}{\text{s}^2})}{998 \frac{\text{kg}}{\text{m}^3} (0.001\text{m}) (9.81 \frac{\text{m}}{\text{s}^2})} = 0.0118 \text{ m} \quad \left(\frac{2(5.8 \times 10^{-2} \frac{\text{kg} \cdot \text{m}}{\text{s}^2})}{958 \frac{\text{kg}}{\text{m}^3} (0.001\text{m}) (9.81 \frac{\text{m}}{\text{s}^2})} \right)$$

$$\frac{2(5.2 \times 10^{-2} \frac{\text{kg} \cdot \text{m}}{\text{s}^2})}{998 \frac{\text{kg}}{\text{m}^3} (0.0001\text{m}) (9.81 \frac{\text{m}}{\text{s}^2})} = 0.1124 \text{ m} \quad = 0.0123 \text{ m}$$

$$\frac{2(5.8 \times 10^{-2} \frac{\text{kg} \cdot \text{m}}{\text{s}^2})}{958 \frac{\text{kg}}{\text{m}^3} (0.0001\text{m}) (9.81 \frac{\text{m}}{\text{s}^2})} = 0.1234 \text{ m}$$

20°C

25°C

Laidler (1^{ra} edición)

18.17)

$$\gamma = 7.27 \times 10^{-2} \text{ N/m} \quad \rho = 0.998 \text{ g/cm}^3 \quad \theta = 0^\circ \quad g = 9.81 \text{ m/s}^2$$

$\hookrightarrow 998 \text{ kg/m}^3$

- a) Calcular elevación del agua en capilares de 1 mm de radio
b) Calcular elevación del agua en capilares de 10^{-3} cm radio

Para a):

$$h = \frac{2\gamma \cos \theta}{\rho g r} = \frac{2(7.27 \times 10^{-2})(\cos 0^\circ)}{(998)(9.81)(0.001)} = 0.1485 \text{ m}$$

Para b):

$$\begin{aligned} \hookrightarrow 1.485 \times 10^{-2} \text{ m} \\ \hookrightarrow 1.485 \text{ cm} \end{aligned}$$

$$\frac{2(7.27 \times 10^{-2})(\cos 0^\circ)}{998(9.81)(1 \times 10^{-5})} = 1.4851 \text{ m}$$

18.21)

$$h_1 = 1.5 \text{ cm} \quad \theta = 0^\circ \quad \gamma_2 = \frac{1}{2} \gamma_1 \quad \rho_2 = \frac{1}{2} \rho_1 \quad g = 9.81 \text{ m/s}^2$$

$$h_2 = ?$$

18.25)

$$A = \frac{1}{2} \text{ acre} \rightarrow 1 \text{ acre} = 4840 \text{ yd}^2 \rightarrow 1 \text{ yd} = 0.915 \text{ m}$$

$$V = 1 \text{ cm}^3 \text{ espesor} = P$$

$$4840(0.915)^2 = 4052 \text{ m}^2 \quad ; \quad \frac{1}{2} \text{ acre} = 2026 \text{ m}^2$$

$$\frac{1 \times 10^{-6} \text{ m}^3}{2026 \text{ m}^2} = 4.9358 \times 10^{-10} \text{ m}$$

$$1 \text{ cm}^3 = 1 \times 10^{-6} \text{ m}^3$$

18.26)

$$T = 15^\circ \text{C}$$

$A = \text{cm}^2 \text{ } \mu\text{g}^{-1}$	5.1	28.2	507	1070	2200	11,000
$\delta = 10^{-3} \text{ N/m}$	30	0.3	0.2	0.1	0.05	0.01

Estimar el peso molecular y el area por molecula cuando la pelicula este totalmente comprimida

$$1.11 \times 10^{11} \text{ N m/kg} = (J/kg)$$

$$2.3145(288.15) = 2,395.823 \text{ J/mol}$$

$$PM = \frac{2,395.823 \text{ J/mol}}{1.11 \times 10^{11} \text{ J/kg}} = 0.2158 \text{ kg/mol} \rightarrow 215.8 \text{ g/mol}$$

$$1 \mu\text{s} = \frac{6.022 \times 10^{23} (10^{-6})}{216} = 2.7379 \times 10^{15} \text{ moleculas}$$

$$A_{\text{molecula}} = \frac{5.7 \text{ cm}^2}{2.7879 \times 10^{15}} = 2.04415 \times 10^{-15} \text{ cm}^2/\text{molecula}$$

$$= 0.2044 \text{ nm}^2/\text{molecula}$$

$$18.18) \ln \frac{P}{P_0} = \frac{2\gamma \bar{v}}{rRT}$$

P = Presión de vapor de las gotitas

P_0 = Presión de vapor en sup. plana

r = radio de las gotas

$$m = 10^{-12} \text{ g}$$

$$\gamma = 7.27 \times 10^{-2} \text{ N m}^{-1}$$

$$\rho = 0.998 \text{ g/cm}^3$$

$$M = 18 \text{ g/mol}$$

$$T = 20^\circ \text{C}$$

$$\rho = \frac{m}{V_{\text{gota}}}$$

$$V_{\text{gota}} = \frac{m}{\rho} = \frac{10^{-12} \text{ g}}{0.998 \text{ g/cm}^3} = 1.002 \times 10^{-12} \text{ cm}^3$$

$$V_{\text{gota}} = \frac{4}{3} \pi r^3$$

$$r = \sqrt[3]{\frac{3 V_{\text{gota}}}{4 \pi}} \rightarrow \sqrt[3]{\frac{3(1.002 \times 10^{-12}) \text{ cm}^3}{4 \pi}}$$

$$r = 6.208 \times 10^{-5} \text{ cm} \left(\frac{1 \text{ m}}{100 \text{ cm}} \right) = 6.208 \times 10^{-7} \text{ m}$$

$$\rho = \frac{M}{\bar{v}} \rightarrow \bar{v} = \frac{M}{\rho} = \frac{18 \text{ g/mol}}{0.998 \text{ g/cm}^3}$$

$$L > 2.041 \frac{\text{cm}^2}{\text{mol}} \left(\frac{\text{Lm}^3}{10^6 \text{ cm}^3} \right) = 1.804 \times 10^{-5} \text{ m}^3/\text{mol}$$

$$\frac{P}{P_0} = \exp \left[\frac{2\gamma \bar{v}}{rRT} \right]$$

$$\frac{2\gamma \bar{v}}{rRT} = \frac{2(7.27 \times 10^{-2} \text{ N m}^{-1})(1.804 \times 10^{-5} \text{ m}^3/\text{mol})}{(6.208 \times 10^{-7} \text{ m})(8.314 \frac{\text{J}}{\text{mol K}})(293.15 \text{ K})}$$

$$L > 1.7345 \times 10^{-3}$$